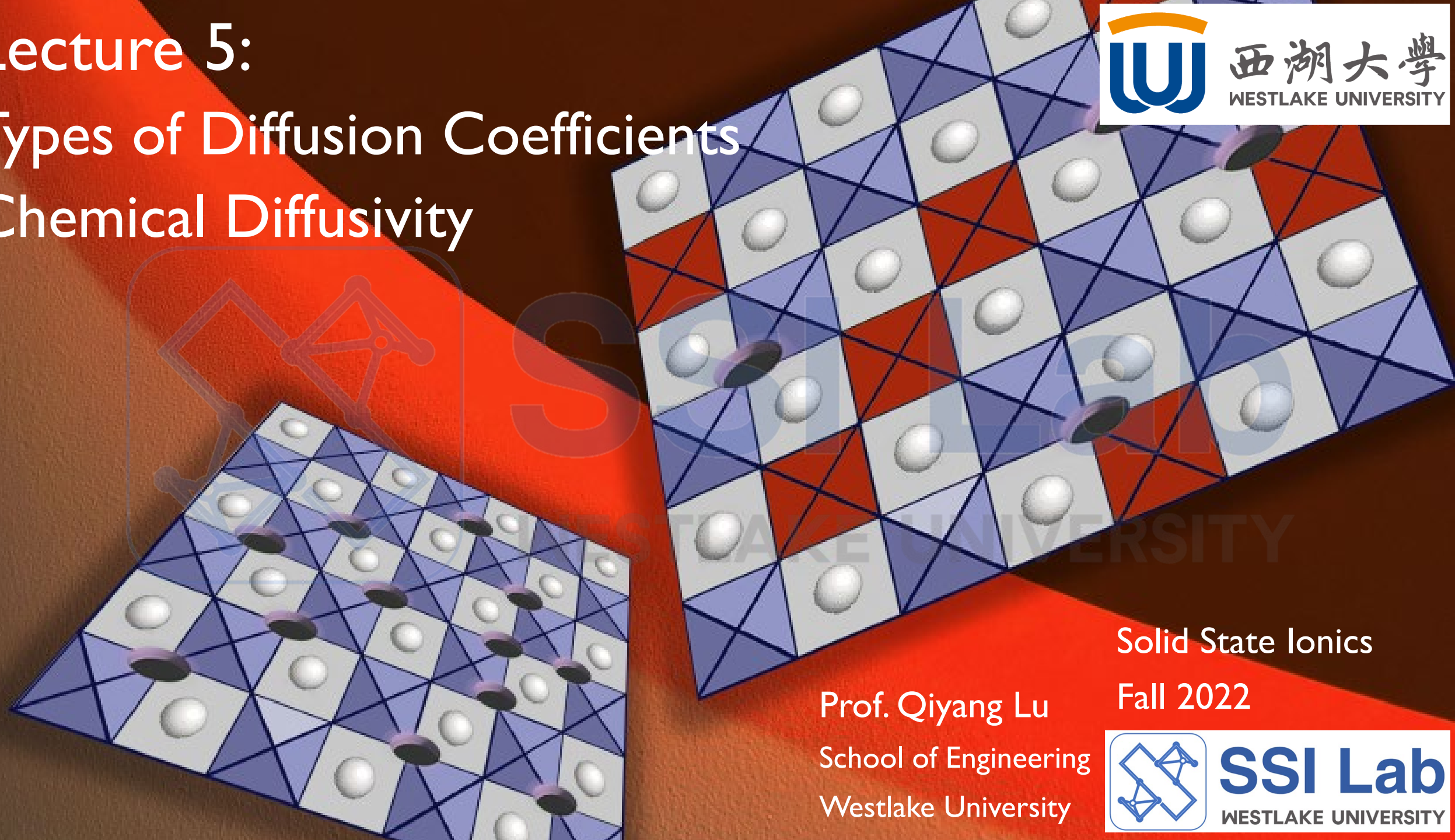


# Lecture 5:

## Types of Diffusion Coefficients

### Chemical Diffusivity



Solid State Ionics

Fall 2022

Prof. Qiyang Lu

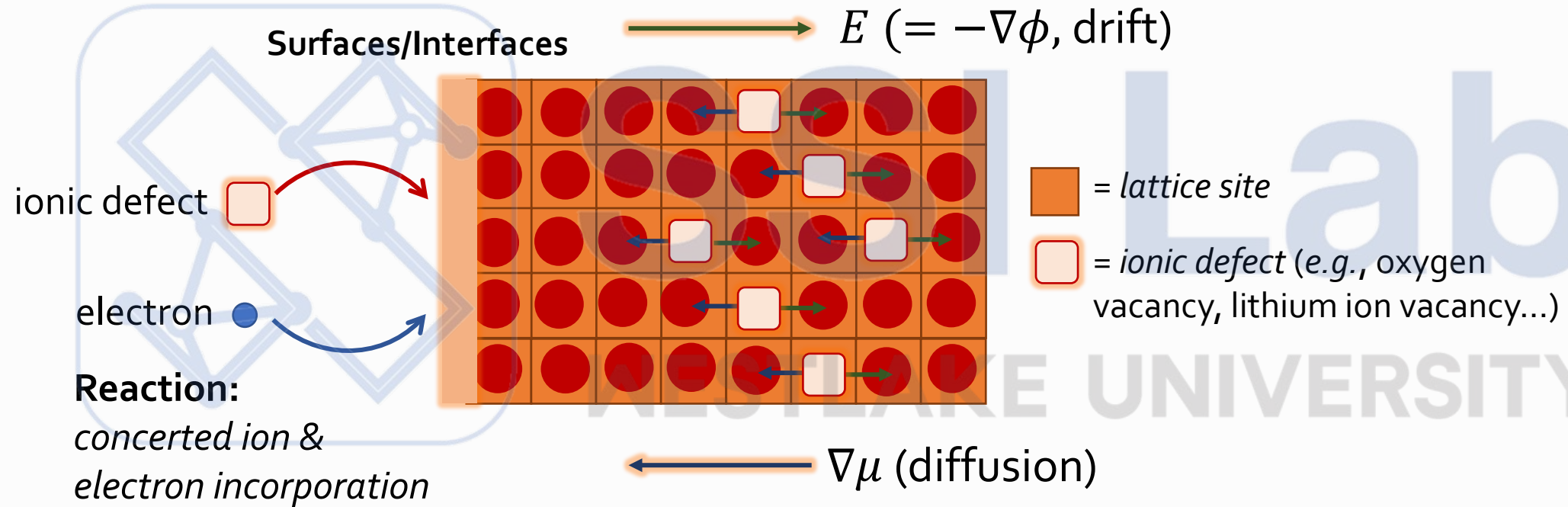
School of Engineering

Westlake University



**SSI Lab**  
WESTLAKE UNIVERSITY

# Diffusion and reactions in solid states w/ the picture of ionic defects



**Ion motion:** *drift + diffusion*  
(similar to electrons/holes in semiconductor physics)

# Things we will discuss in this lecture

## Type of diffusivities:

- What are the different types of diffusivities?
- What physical mechanism and concept does each diffusivity describe?

## Chemical diffusivity:

- What physical process does the chemical diffusion describe?
- What are the key factors that govern the chemical diffusivity?



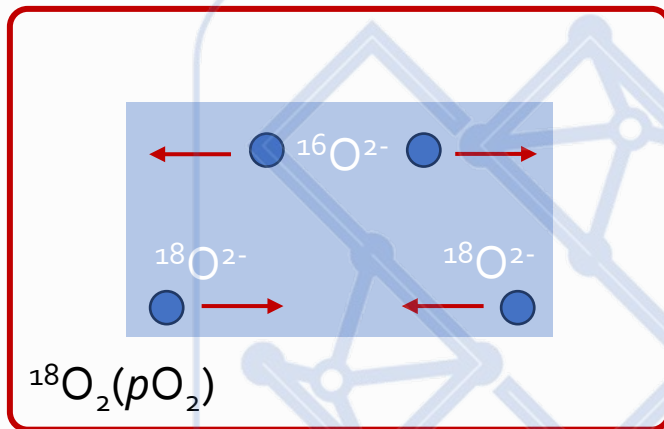
**Goal of this lecture:** you should be able to answer the questions above by the end of this lecture : )

***A test on your intuition:*** Is the diffusion coefficient dependent on the concentration of ionic defects?

# Types of diffusivities (or diffusion coefficients)

We can measure *phenomenological* diffusivity by using the three different experiments:

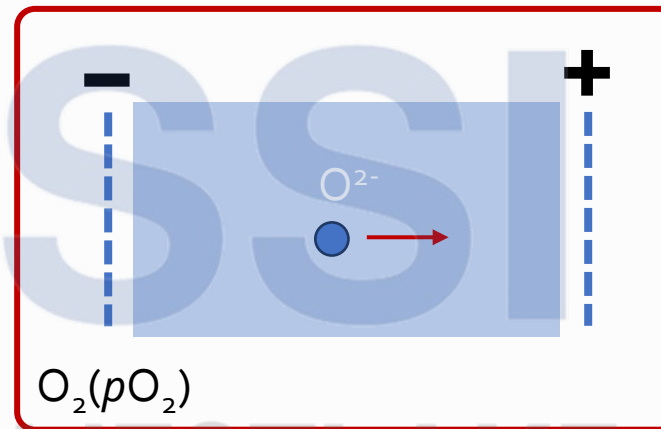
Tracer experiment



Tracer diffusivity

$$D_{\text{O}^{2-}}^*$$

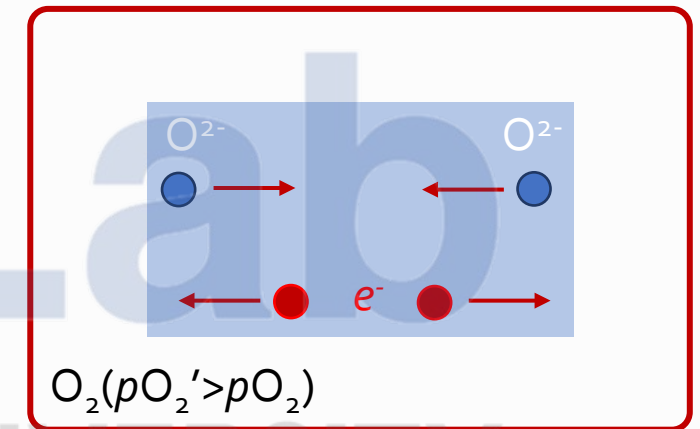
Stationary conductivity experiment



Self-diffusivity

$$D_{\text{O}^{2-}}^q$$

Chemical diffusion experiment



Chemical diffusivity

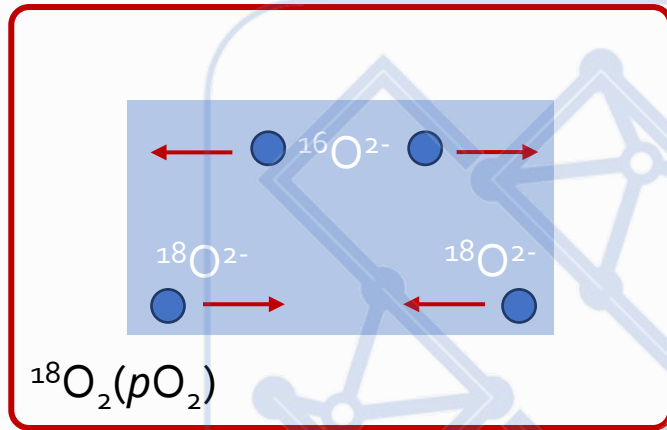
$$D_{\text{O}}^{\delta}$$

No compositional (stoichiometric) change

Composition (stoichiometry  $\delta$ ) changes

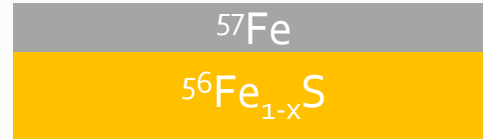
# Tracer diffusivity: isotope exchange profile

Tracer experiment

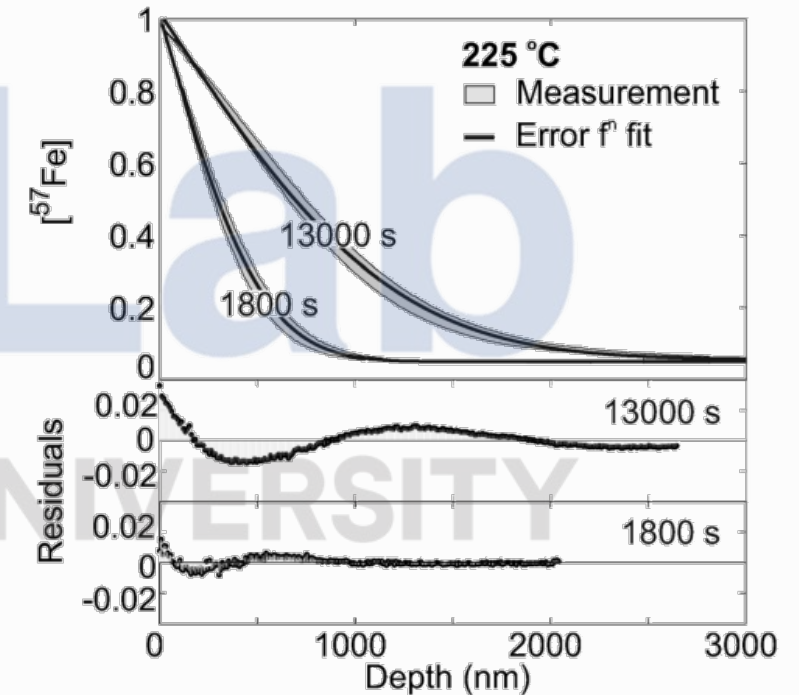
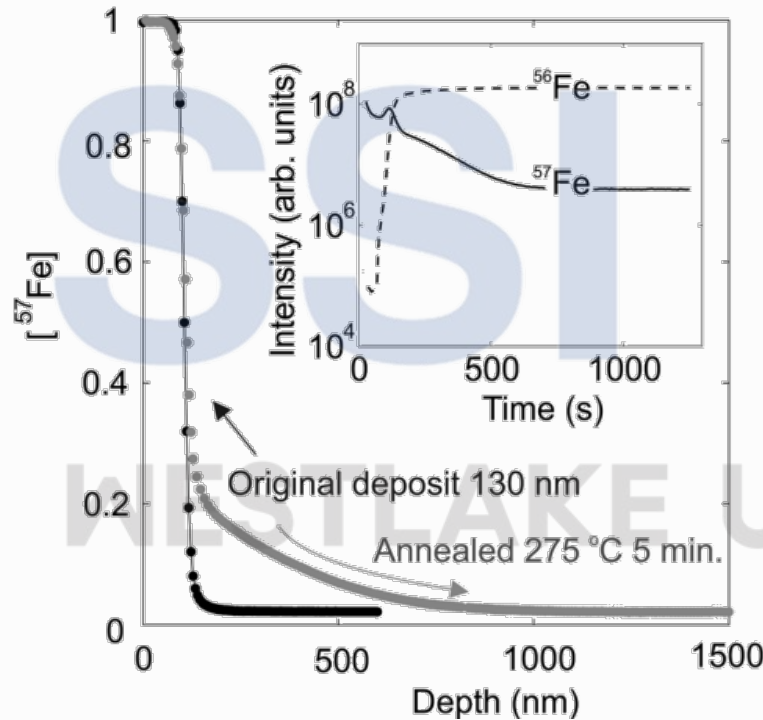
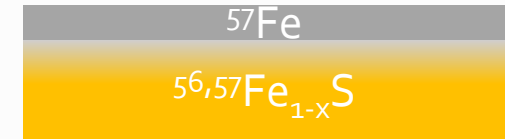


Tracer diffusivity

$$D_{\text{O}^{2-}}^*$$



anneal

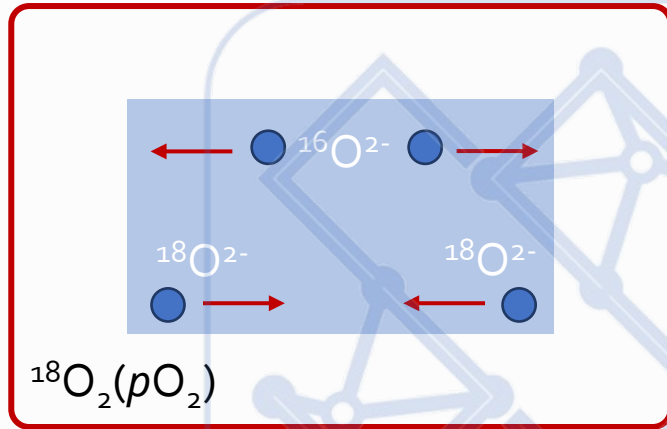


- $^{57}\text{Fe}$  isotope profile measured by using secondary-ion mass spectrometry (SIMS)
- Concentration profile modeled by solving semi-infinite diffusion equation

$$c(x, t) = c_0 \left( 1 - \text{erf} \left( \frac{x}{4D^*t} \right) \right)$$

# Tracer diffusivity: isotope exchange profile

Tracer experiment

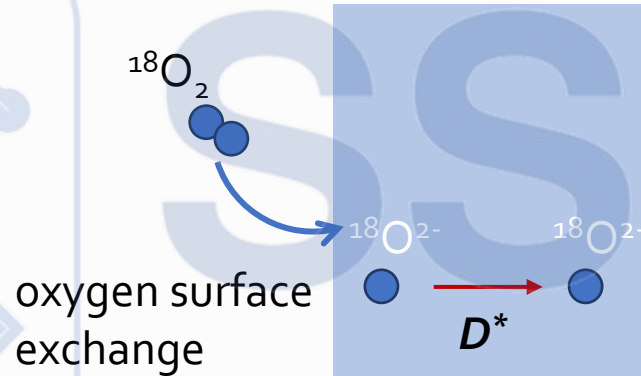


Tracer diffusivity

$$D_{\text{O}^{2-}}^*$$

Fick's 2<sup>nd</sup> Law:

$$\frac{\partial c(x, t)}{\partial t} = D^* \frac{\partial^2 c(x, t)}{\partial x^2}$$



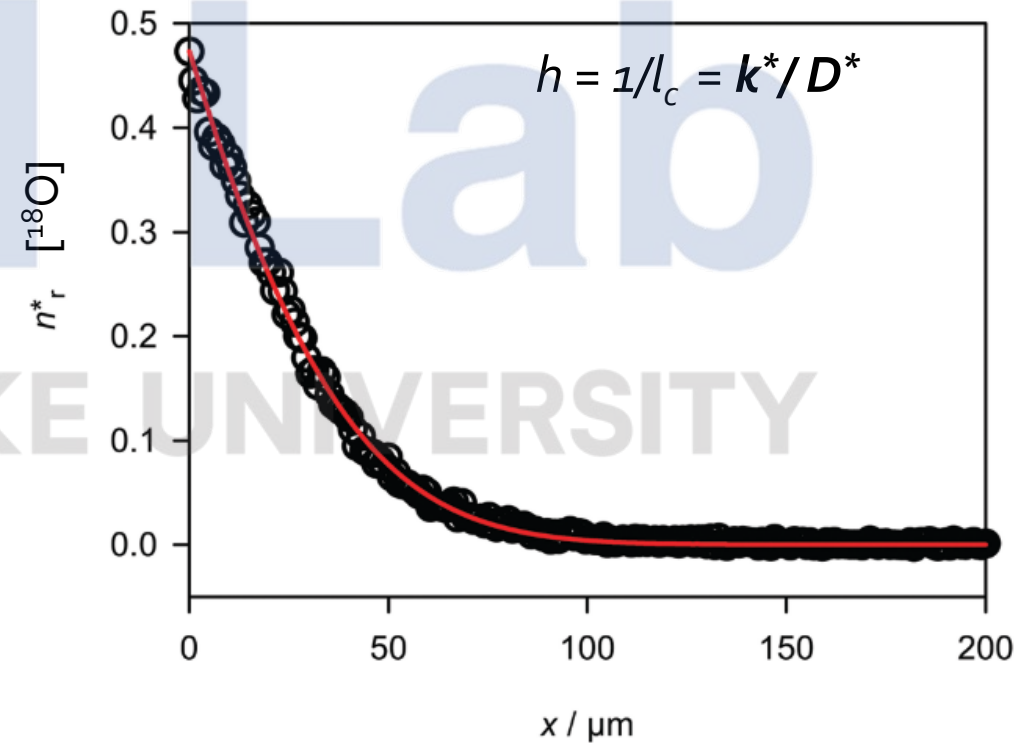
rate constant  $k^*$

$k^*$ : unit cm/s

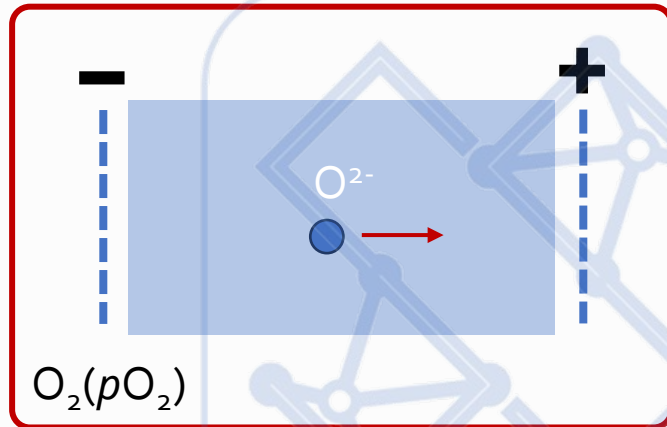
$D^*$ : unit cm<sup>2</sup>/s

$$\text{Critical length } l_c = D^*/k^*$$

$$\frac{n^*(x) - n_{\text{bg}}^*}{n_g^* - n_{\text{bg}}^*} = \text{erfc}\left(\frac{x}{2\sqrt{D^*t_{\text{ex}}}}\right) - \exp(hx + h^2 D^* t_{\text{ex}}) \times \text{erfc}\left(\frac{x}{2\sqrt{D^*t_{\text{ex}}}} + h\sqrt{D^*t_{\text{ex}}}\right)$$



Stationary conductivity experiment



Self-diffusivity

$$D_{O^{2-}}^q$$

Consider **Nernst-Einstein** relation

$$\frac{D}{M} = \frac{RT}{zF}$$

$$\sigma = c zF \frac{D}{RT} = c \frac{z^2 F^2}{RT} D$$

Therefore, we can get diffusivity by measuring ionic conductivity.

We have:

$$D = \frac{RT}{z^2 F^2} \frac{\sigma}{c}$$

Confusing question: *which concentration should we plug in here?*

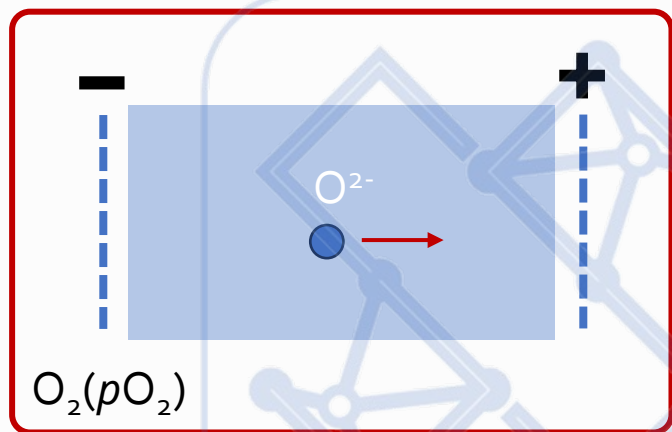
$$D_{O^{2-}}^q = \frac{RT}{4F^2} \frac{\sigma_{O^{2-}}}{c_{O^{2-}}}$$

Oxide ion ( $O^{2-}$ ) concentration  
(**NOT** defect concentration)

$q$ : charge transport

# Self-diffusivity: steady-state conductivity measurement

Stationary conductivity experiment



Self-diffusivity

$$D_{O^{2-}}^q$$

$$D_{O^{2-}}^q = \frac{RT}{4F^2} \frac{\sigma_{O^{2-}}}{c_{O^{2-}}}$$

$q$ : charge transport

Oxide ion ( $O^{2-}$ ) concentration  
(**NOT** defect concentration)

In reality, the  $O^{2-}$  conductivity is contributed by defects (either oxygen vacancies  $V_O^{\bullet\bullet}$  or oxygen interstitials  $O_i''$ ).

If we assume that oxygen interstitials  $O_i''$  are the major oxygen ionic defects,

we have:

$$\sigma_{O^{2-}} = \sigma_{O_i''} = 2Fc_{O_i''}M_{O_i''}$$

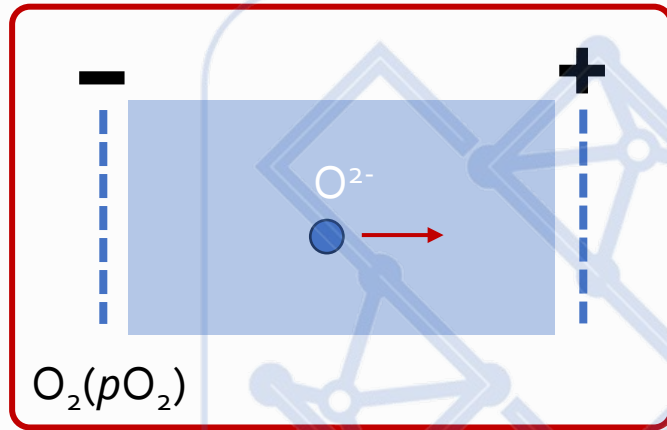
$$D_{O^{2-}}^q = \frac{RT}{4F^2} \frac{\sigma_{O^{2-}}}{c_{O^{2-}}} = \frac{RT}{4F^2} \frac{\sigma_{O_i''}}{c_{O_i''}} \frac{c_{O_i''}}{c_{O^{2-}}} = D_{O_i''} \frac{c_{O_i''}}{c_{O^{2-}}}$$

$$D_{O^{2-}}^q = D_{O_i''} \frac{c_{O_i''}}{c_{O^{2-}}} = x_{O_i''} D_{O_i''}$$

Fraction of oxygen interstitials  $O_i''$

# Self-diffusivity: steady-state conductivity measurement

Stationary conductivity experiment



Self-diffusivity

$$D_{O^{2-}}^q$$

$$D_{O^{2-}}^q = D_{O_i''} \frac{c_{O_i''}}{c_{O^{2-}}} = x_{O_i''} D_{O_i''}$$

Fraction of oxygen interstitials  $O_i''$

Since  $x_{O_i''} = c_{O_i''}/c_{O^{2-}}$  is far less than 1

$$D_{O_i''} \gg D_{O^{2-}}^q$$

The self-diffusivity of defect species is *much higher* than that of ionic species.

Contain information on both ion migration and defect formation

$$D_{O^{2-}}^q = x_{O_i''} D_{O_i''}$$

Related to defect formation

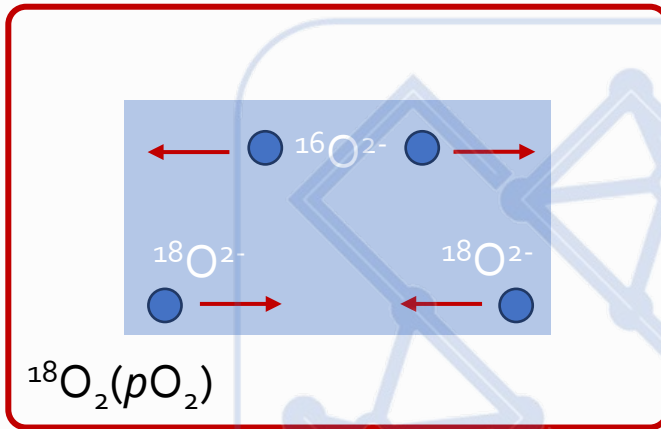
$$\propto \exp\left(-\frac{\Delta H_f}{k_B T}\right)$$

Reflect the "true" mechanism of ion migration

$$\propto \exp\left(-\frac{\Delta H_{mig}}{k_B T}\right)$$

# Relationship between tracer diffusivity and self-diffusivity

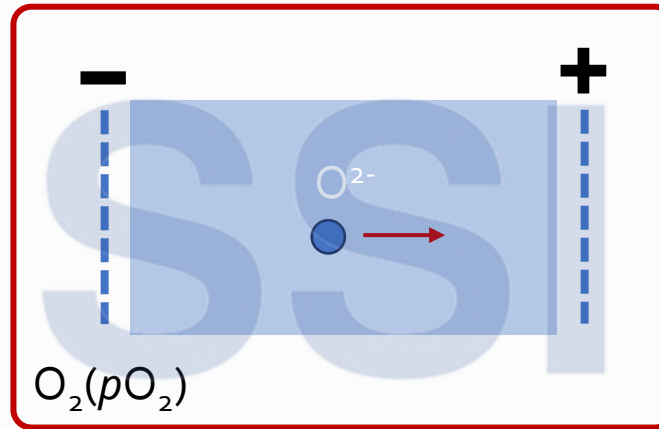
Tracer experiment



Tracer diffusivity

$$D_{\text{O}^{2-}}^*$$

Stationary conductivity experiment



Self-diffusivity

$$D_{\text{O}^{2-}}^q$$

No compositional (stoichiometric) change

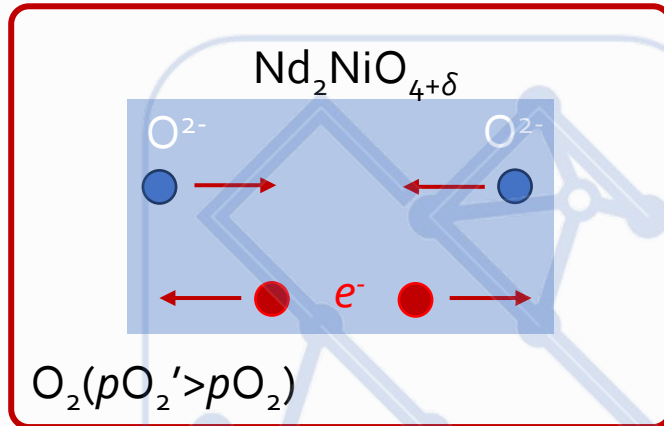
Tracer diffusivity and self-diffusivity are usually on the same order of magnitude, since they both describe the process **without** compositional changes.

$$D_{\text{O}^{2-}}^* = H_{\text{O}^{2-}} D_{\text{O}^{2-}}^q$$

Haven ratio

- *Haven ratio* mainly describes the correlations between each hops.
- $H_{\text{O}^{2-}}$  is usually of the order of 1

## Chemical diffusion experiment

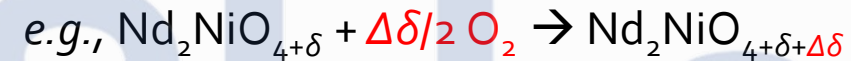


Chemical diffusivity

$$D_O^\delta$$

Composition (stoichiometry  $\delta$ ) changes

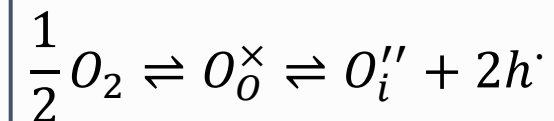
Very different from tracer diffusivity and self-diffusivity, chemical diffusion describe the process that involves ***compositional or stoichiometric changes***.



In order to change oxygen stoichiometry ( $\Delta\delta$ ), oxide ions  $\text{O}^{2-}$  and electrons  $e^-$  must diffuse to opposite directions, to maintain ***charge neutrality***.

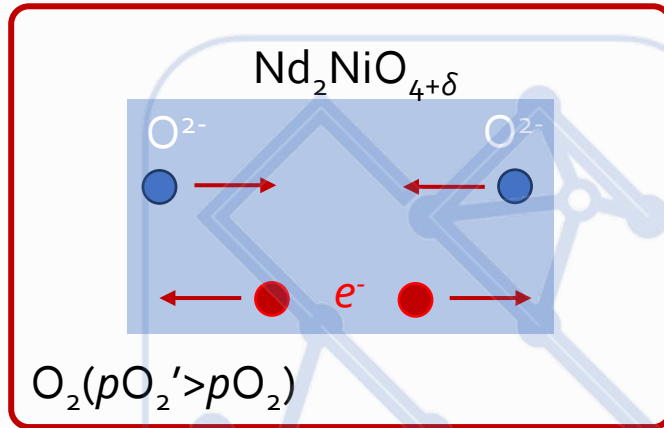
Therefore, chemical diffusivity is called ***ambipolar diffusivity***, meaning that chemical diffusion involves the motion of ***two charged species***.

In  $\text{Nd}_2\text{NiO}_{4+\delta}$  the change of oxygen stoichiometry can be expressed by the defect chemical reaction below:



# Chemical diffusivity: stoichiometric changes

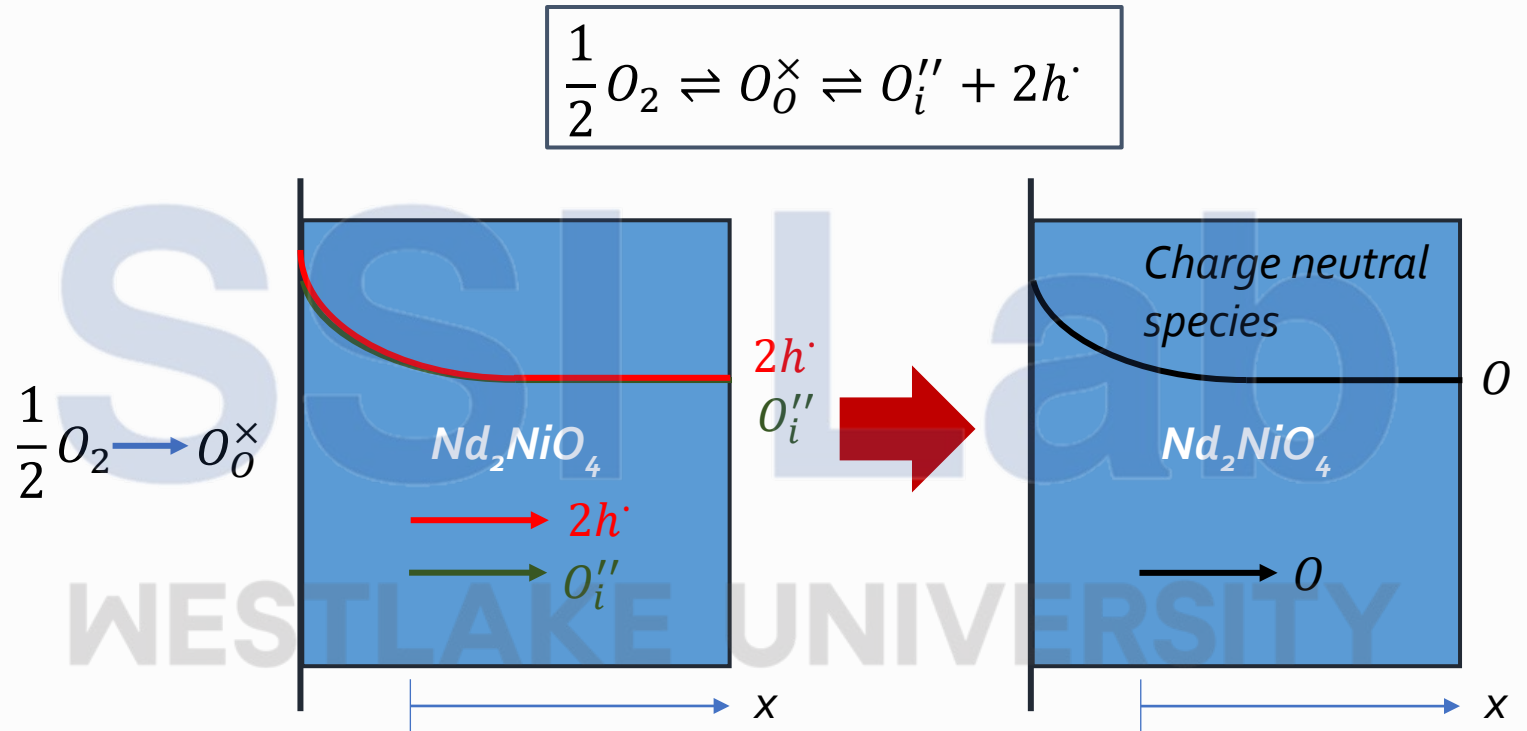
Chemical diffusion experiment



Chemical diffusivity

$$D_O^\delta$$

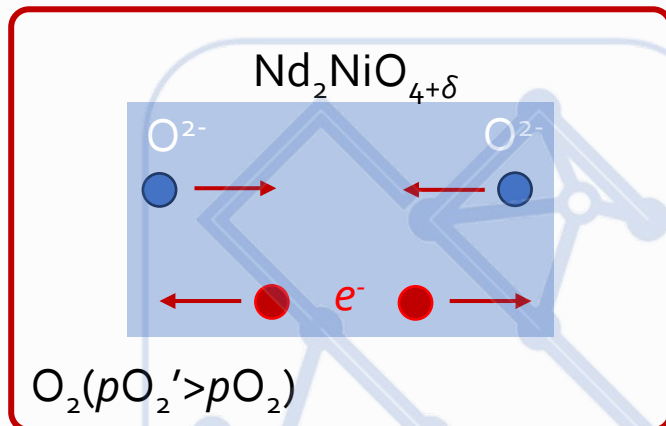
Composition (stoichiometry  $\delta$ ) changes



**Our goal:** find the expression of chemical diffusivity based on properties of defects ( $\text{O}_\text{i}''$  &  $\text{h}^\cdot$ ) so that we can use Fick's law to predict the concentration profile, i.e.:

$$J_\text{O} = -D_\text{O}^\delta \nabla c_\text{O} \text{ or } J_\text{O} = -D_\text{O}^\delta \frac{\partial c_\text{O}}{\partial x} (1\text{D})$$

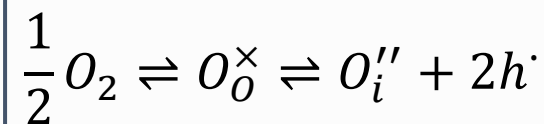
Chemical diffusion experiment



Chemical diffusivity

$$D_O^\delta$$

Composition (stoichiometry  $\delta$ ) changes



Flux of oxygen interstitials:

$$J_{O_i''} = -\frac{\sigma_{O_i''}}{4F^2} \nabla \tilde{\mu}_{O_i''} = -\frac{\sigma_{O_i''}}{4F^2} (\nabla \mu_{O_i''} - 2F \nabla \phi)$$

Flux of holes:

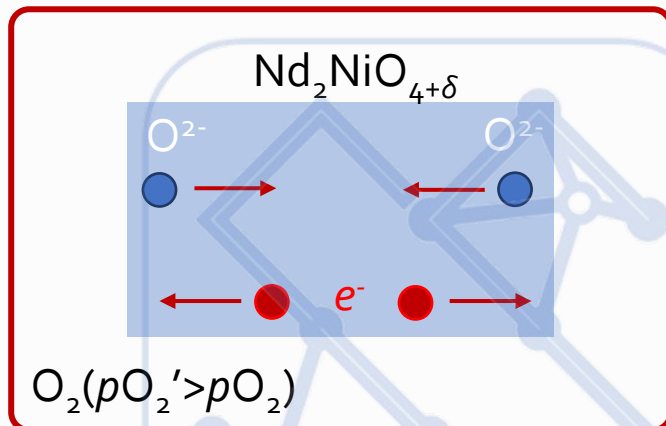
$$J_{h^\cdot} = -\frac{\sigma_{h^\cdot}}{F^2} \nabla \tilde{\mu}_{h^\cdot} = -\frac{\sigma_{h^\cdot}}{F^2} (\nabla \mu_{h^\cdot} + F \nabla \phi)$$

To satisfy the local electro-neutral condition (we will discuss why it holds):

$$J_{O_i''} = \frac{1}{2} J_{h^\cdot}$$

$$\frac{\sigma_{O_i''}}{4F^2} (\nabla \mu_{O_i''} - 2F \nabla \phi) = \frac{\sigma_{h^\cdot}}{2F^2} (\nabla \mu_{h^\cdot} + F \nabla \phi) \rightarrow \frac{\sigma_{O_i''}}{4F^2} \nabla \mu_{O_i''} - \frac{\sigma_{h^\cdot}}{2F^2} \nabla \mu_{h^\cdot} = \frac{\sigma_{O_i''} + \sigma_{h^\cdot}}{2F} \nabla \phi$$

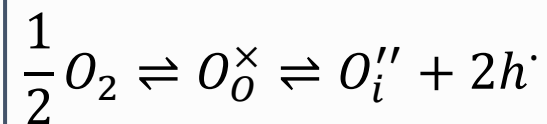
Chemical diffusion experiment



Chemical diffusivity

$$D_O^\delta$$

Composition (stoichiometry  $\delta$ ) changes



$$\frac{\sigma_{O_i''}}{4F^2} \nabla \mu_{O_i''} - \frac{\sigma_{h^\cdot}}{2F^2} \nabla \mu_{h^\cdot} = \frac{\sigma_{O_i''} + \sigma_{h^\cdot}}{2F} \nabla \phi$$

$$\begin{aligned} J_O = J_{O_i''} &= -\frac{\sigma_{O_i''}}{4F^2} (\nabla \mu_{O_i''} - 2F \nabla \phi) = -\frac{\sigma_{O_i''}}{4F^2} \nabla \mu_{O_i''} + \frac{\sigma_{O_i''}}{2F} \nabla \phi \\ &= -\frac{\sigma_{O_i''}}{4F^2} \nabla \mu_{O_i''} + \frac{\sigma_{O_i''}}{\sigma_{O_i''} + \sigma_{h^\cdot}} \left( \frac{\sigma_{O_i''}}{4F^2} \nabla \mu_{O_i''} - \frac{\sigma_{h^\cdot}}{2F^2} \nabla \mu_{h^\cdot} \right) \end{aligned}$$

$$J_O = -\frac{1}{4F^2} \frac{\sigma_{h^\cdot} \sigma_{O_i''}}{\sigma_{O_i''} + \sigma_{h^\cdot}} (\nabla \mu_{O_i''} + 2 \nabla \mu_{h^\cdot})$$

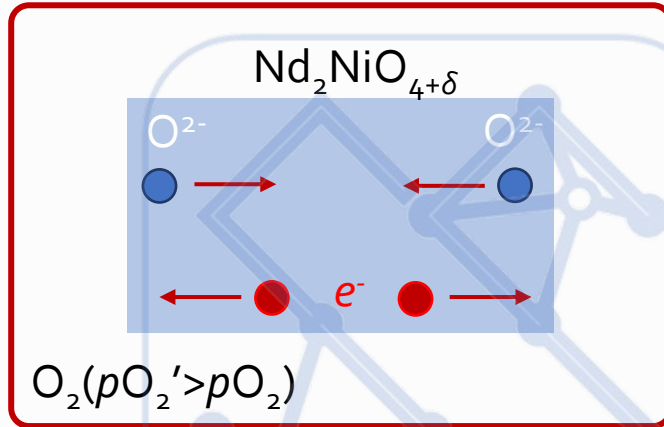
If we denote:  $\mu_O = \mu_{O_i''} + 2\mu_{h^\cdot}$

$$J_O = -\frac{1}{4F^2} \frac{\sigma_{h^\cdot} \sigma_{O_i''}}{\sigma_{O_i''} + \sigma_{h^\cdot}} \nabla \mu_O = -\frac{1}{4F^2} \sigma_O^\delta \frac{\partial \mu_O}{\partial c_O} \nabla c_O$$

$$\sigma_O^\delta = \frac{\sigma_{h^\cdot} \sigma_{O_i''}}{\sigma_{O_i''} + \sigma_{h^\cdot}}$$

# Chemical diffusivity: stoichiometric changes

Chemical diffusion experiment



Chemical diffusivity

$$D_O^\delta$$

Composition (stoichiometry  $\delta$ ) changes

$$J_O = -\frac{1}{4F^2} \sigma_O^\delta \frac{\partial \mu_O}{\partial c_O} \nabla c_O$$

$$\sigma_O^\delta = \frac{\sigma_h \cdot \sigma_{O_i}''}{\sigma_{O_i}'' + \sigma_h}$$

$$\mu_O = \mu_O^0 + RT \ln a_O$$

activity, dilute limit  $\rightarrow c_O$

$$\frac{\partial \mu_O}{\partial c_O} = \frac{\partial (\mu_{O_i}'' + 2\mu_h)}{\partial c_O}$$

$$D_O^\delta = \frac{1}{4F^2} \sigma_O^\delta \frac{\partial \mu_O}{\partial c_O} = \frac{RT}{4F^2} \frac{\sigma_h \cdot \sigma_{O_i}''}{\sigma_{O_i}'' + \sigma_h} \left( \frac{1}{c_{O_i}''} + \frac{4}{c_h} \right)$$

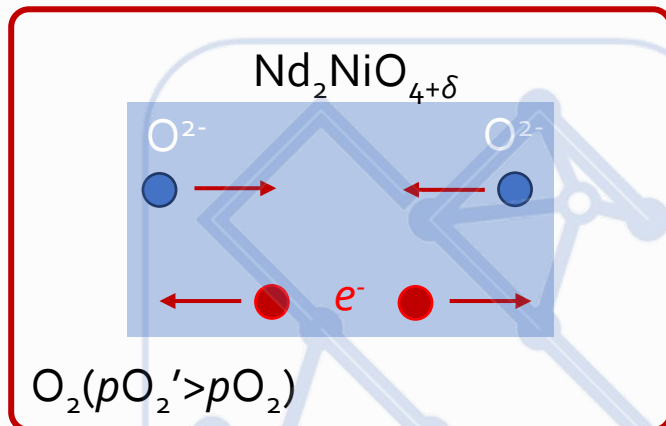
$$(\partial c_O = \partial c_{O_i}'' = \frac{1}{2} \partial c_h)$$

"electrical"

"ionic"

# Chemical diffusivity: stoichiometric changes

Chemical diffusion experiment



Chemical diffusivity

$$D_O^\delta$$

Composition (stoichiometry  $\delta$ ) changes

$$D_O^\delta = \frac{1}{4F^2} \sigma_O^\delta \frac{\partial \mu_O}{\partial c_O} = \frac{1}{4F^2} \underbrace{\frac{\sigma_h \cdot \sigma_{O_i''}}{\sigma_{O_i''} + \sigma_h}}_{\text{"electrical"}} \underbrace{\left( \frac{1}{c_{O_i''}} + \frac{4}{c_h} \right)}_{\text{"ionic"}}$$

(valid at dilute limit)

$$D_O^\delta = \frac{RT}{4F^2} \frac{\sigma_O^\delta}{c_O^\delta}$$

"electrical": harmonic mean **conductivity**

$$\frac{1}{\sigma_O^\delta} = \frac{1}{\sigma_{O_i''}} + \frac{1}{\sigma_h}$$

"ionic": harmonic mean **concentration**

$$\frac{1}{c_O^\delta} = \frac{1}{c_{O_i''}} + \frac{2^2}{c_h}$$

$$\sigma_{O_i''} = 2c_{O_i''} F M_{O_i''} = \frac{RT}{4F^2} c_{O_i''} D_{O_i''}$$

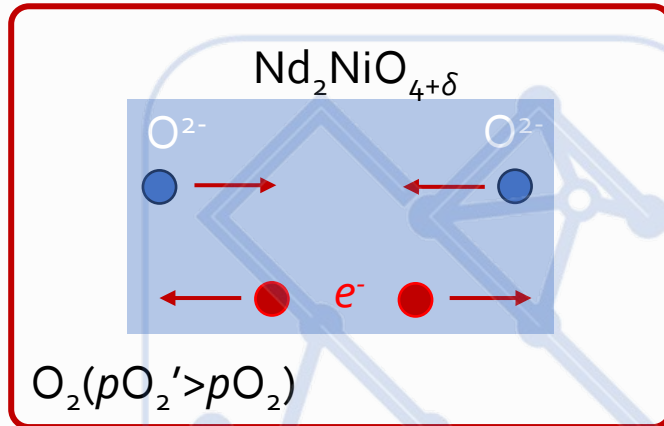
$$\sigma_h = c_h F M_h = \frac{RT}{F^2} c_h D_h$$

$$D_O^\delta = t_h \cdot D_{O_i''} + t_{O_i''} D_h$$

$$t_h = \frac{\sigma_h}{\sigma_{O_i''} + \sigma_h}$$

Transference number

## Chemical diffusion experiment



Chemical diffusivity

$$D_O^\delta$$

Composition (stoichiometry  $\delta$ ) changes

$$D_O^\delta = t_{h\cdot} D_{O_i''} + t_{O_i''} D_{h\cdot}$$

$$t_{h\cdot} = \frac{\sigma_{h\cdot}}{\sigma_{O_i''} + \sigma_{h\cdot}}$$

$$t_{O_i''} = \frac{\sigma_{O_i''}}{\sigma_{O_i''} + \sigma_{h\cdot}}$$

Transference number

If  $\sigma_{h\cdot} \gg \sigma_{O_i''}$ , then  $t_{h\cdot} \rightarrow 1$  and if  $D_{h\cdot}$  is not too large  $\rightarrow D_O^\delta \approx D_{O_i''}$

### Note:

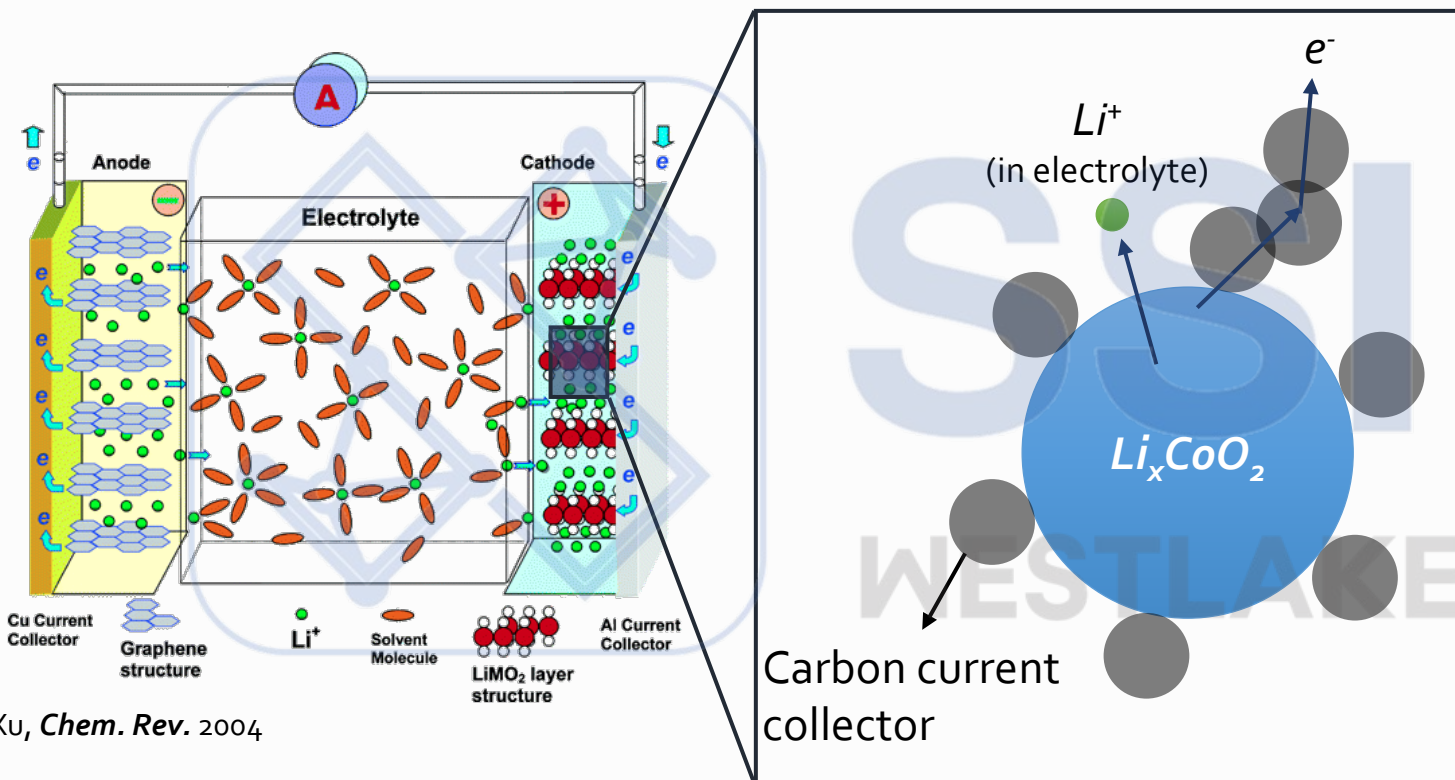
- In this scenario,  $D_O^\delta \approx D_{O_i''} \gg D_{O_2-}^q$  (recall  $D_{O_2-}^q = x_{O_i''} D_{O_i''}$ , while usually  $x_{O_i''} \ll 1$ )
- If the system deviate from the dilute limit, then:

$$D_O^\delta = \Gamma_{h\cdot} t_{h\cdot} D_{O_i''} + \Gamma_{O_i''} t_{O_i''} D_{h\cdot}$$

$\Gamma$ : thermodynamic factor

# Microscopic picture: how is Li intercalated into cathodes?

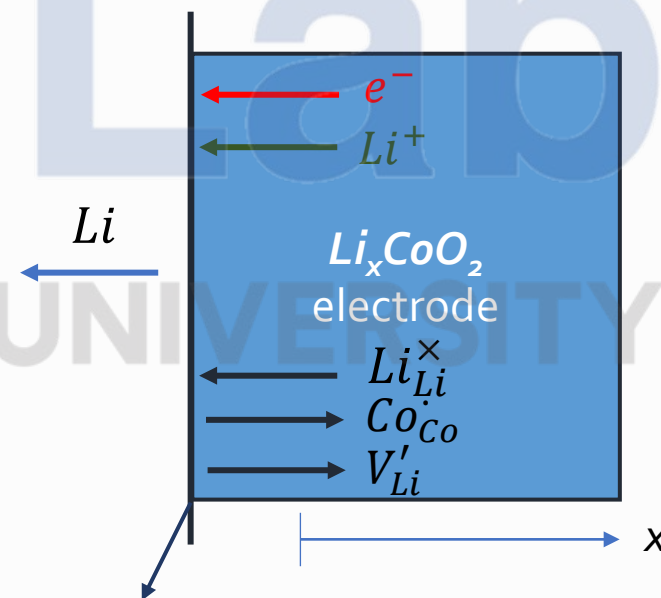
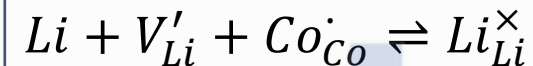
**Question:** how does *Li*-intercalation happen microscopically?



Xu, *Chem. Rev.* 2004



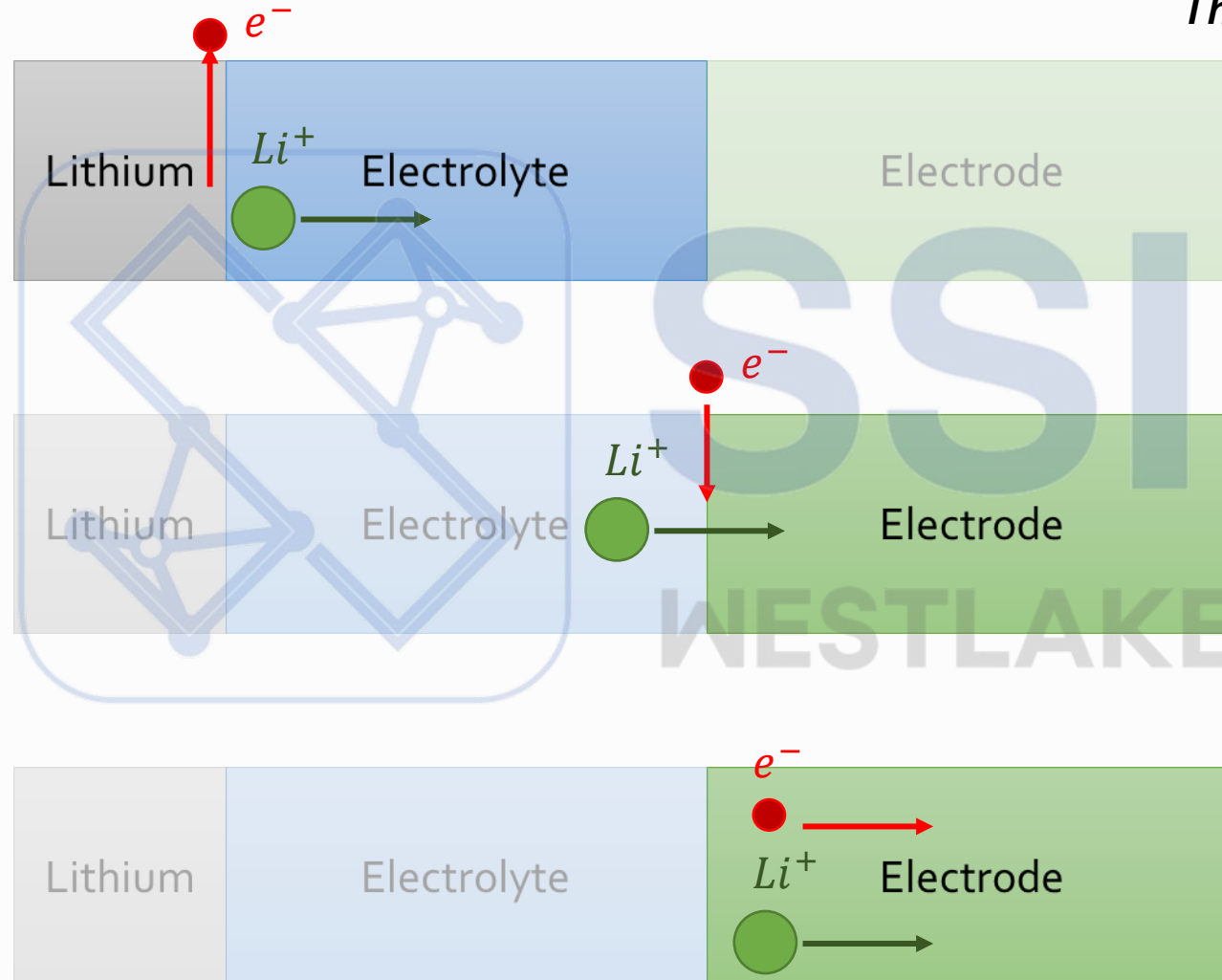
or



$Li_xCoO_2$ /carbon/electrolyte  
interface

# Kinetics and transport in Li-ion batteries

*Three decisive mechanistic steps of a Li-ion battery*



***Ion transport***  
 (through electrolyte)  
 $\tau \sim ns$

***Ion transfer***  
 (at electrolyte/electrode interface)  
 $\tau \sim \mu s$

***Chemical diffusion***  
 (in electrode bulk)  
 $\tau \sim \text{min, hr, yr}$

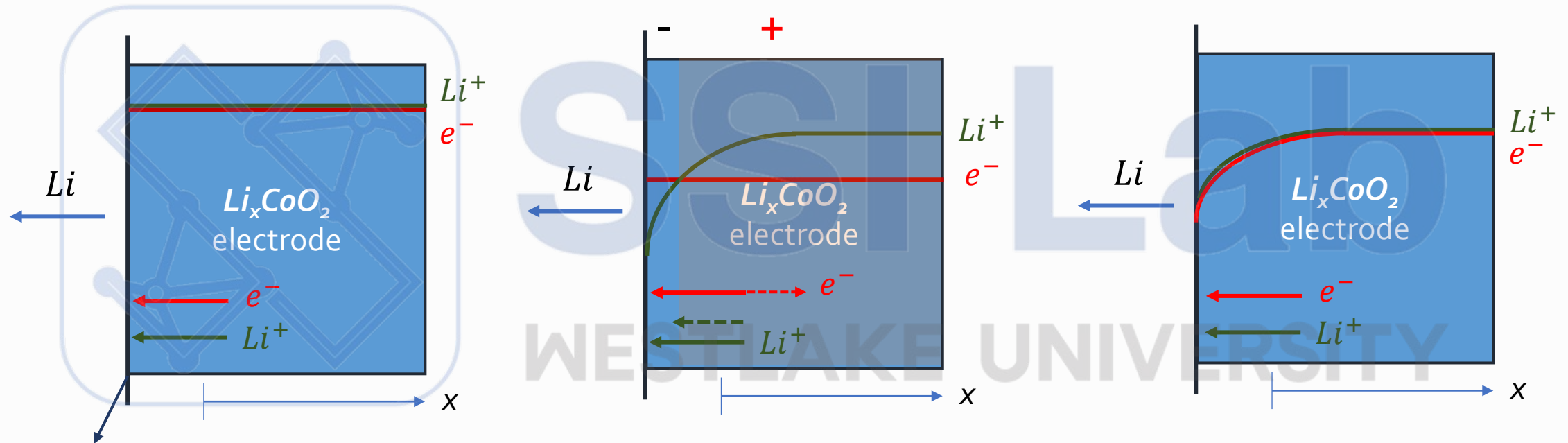
Depend on the size of electrodes!

# Ambipolar diffusion: diffusion process involving both ions and electrons



Usually, the diffusivity (mobility) of **electronic** species (defects) is much faster than that of **ionic** species

$$D_{Li^+} \ll D_{e^-}$$



$Li_xCoO_2$ /carbon/electrolyte  
interface

**Initial state**

Local charge neutral

**Intermediate state  
(imaginary)**

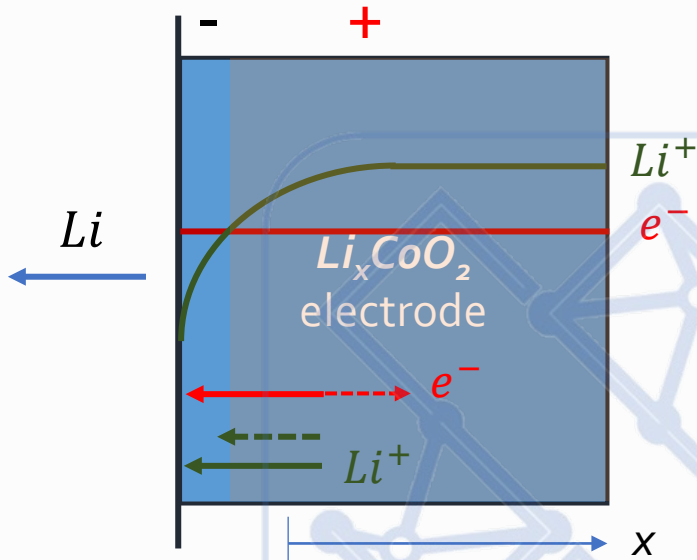
Local charge  $\neq 0$

**Final state**

Local charge neutral

The electric field **slows down** the fast-diffusing species and **speeds up** the slow diffusing species.

Note: the bulk of the sample must be *charge neutral*



**Intermediate state  
(imaginary)**

Local charge  $\neq 0$

This picture on the left is an exaggeration to help you to understand the role of accelerating/decelerating electric field;

In a real world, the **charge neutrality** still holds (except for the interfaces)

We can do a simple back-on-envelope calculation:

$$E = -\frac{\partial \phi}{\partial x}$$

Electric field

$$\frac{\partial E}{\partial x} = \frac{\partial^2 \phi}{\partial x^2} = -\frac{\rho}{\epsilon_0 \epsilon_r}$$

Electrostatic potential

Charge density  $\rho = c \cdot F$

$\epsilon_0$ : vacuum permittivity

$\epsilon_r$ : relative permittivity

**Poisson's equation:** connecting charge with potential

$$\frac{\Delta E}{\Delta x} = -\frac{\rho}{\epsilon_0 \epsilon_r} = -\frac{Fc}{\epsilon_0 \epsilon_r} = -\frac{96500 \text{ C/mol} \times 1 \text{ mol/L}}{8.8 \times 10^{-12} \text{ F/m} \times 10} = 1 \times 10^{18} \text{ V/m}^2 \quad (c = 1 \text{ M})$$

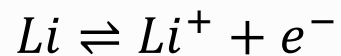
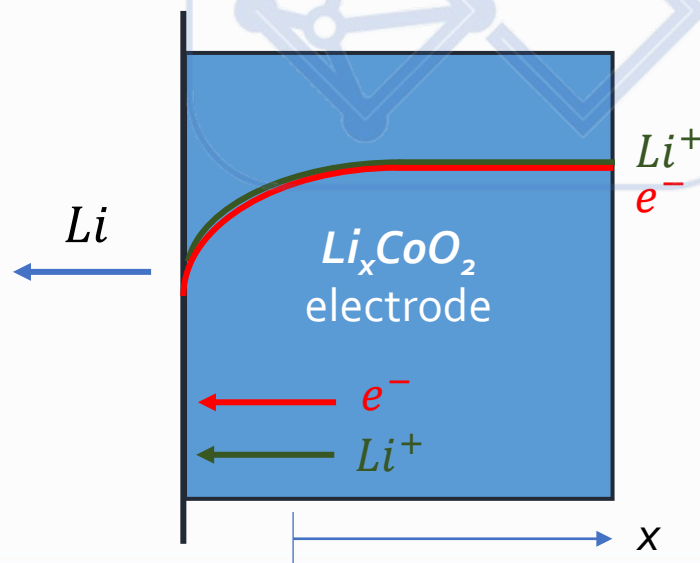
$$\Delta E = \frac{\Delta V}{\Delta x} = 1 \times 10^{18} \text{ V/m}^2 \Delta x \quad \text{If } \Delta x = 1 \text{ nm} \rightarrow \Delta V = 1 \text{ V (!)} \rightarrow \text{Unrealistic}$$

# How to solve for the diffusivity?

## Fick's first law

$$J_{diff, Li} = -D_{Li} \nabla c_{Li}$$

How to express  $D_{Li}$  as a function of  $D_{Li^+}$  and  $D_{e^-}$ ?



Key equation: local equilibrium  $\mu_{Li} = \tilde{\mu}_{e^-} + \tilde{\mu}_{Li^+}$

Flux:  $J_i = -\frac{\sigma_i}{z_i^2 F^2} \nabla \tilde{\mu}_i$

Ionic flow:  $J_{Li^+} = -\frac{\sigma_{Li^+}}{F^2} \nabla \tilde{\mu}_{Li^+}$

Electronic flow:  $J_{e^-} = -\frac{\sigma_{e^-}}{F^2} \nabla \tilde{\mu}_{e^-}$

At steady state:  $J_{Li} = J_{Li^+} = J_{e^-}$

Nernst-Einstein relation:

$$\frac{D_i c_i}{RT} = \frac{\sigma_i}{z_i^2 F^2}$$

$$\mu_{Li} = \tilde{\mu}_{e^-} + \tilde{\mu}_{Li^+} \longrightarrow \nabla \mu_{Li} = \nabla \tilde{\mu}_{e^-} + \nabla \tilde{\mu}_{Li^+}$$

$$J_{Li^+} = J_{e^-} \longrightarrow \sigma_{Li^+} \nabla \tilde{\mu}_{Li^+} = \sigma_{e^-} \nabla \tilde{\mu}_{e^-}$$

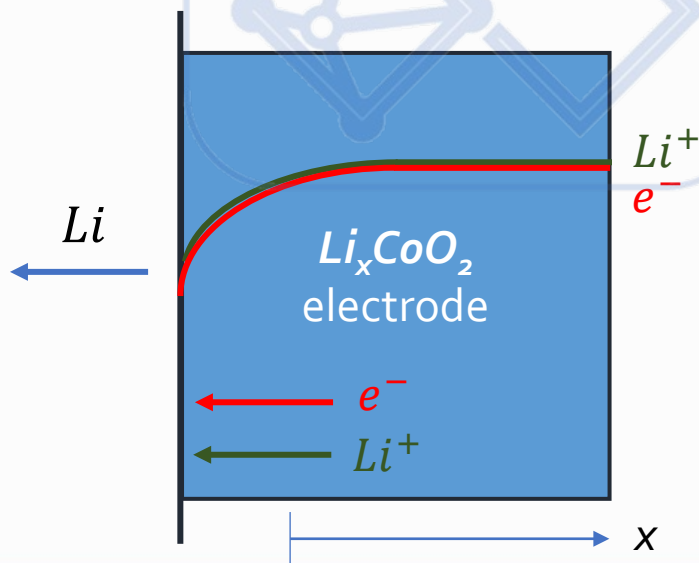
$$\nabla \mu_{Li} = \left(1 + \frac{\sigma_{e^-}}{\sigma_{Li^+}}\right) \nabla \tilde{\mu}_{e^-}$$

# How to solve for the diffusivity?

## Fick's first law

$$J_{diff, Li} = -D_{Li} \nabla c_{Li}$$

How to express  $D_{Li}$  as a function of  $D_{Li^+}$  and  $D_{e^-}$ ?



$$\nabla \mu_{Li} = \left(1 + \frac{\sigma_{e^-}}{\sigma_{Li^+}}\right) \nabla \tilde{\mu}_{e^-}$$

$$J_{Li} = J_{e^-} = -\frac{\sigma_{e^-}}{F^2} \nabla \tilde{\mu}_{e^-} = -\frac{1}{F^2} \frac{\sigma_{e^-} \sigma_{Li^+}}{\sigma_{e^-} + \sigma_{Li^+}} \nabla \mu_{Li}$$

$$J_{Li} = -\frac{1}{F^2} \frac{\sigma_{e^-} \sigma_{Li^+}}{\sigma_{e^-} + \sigma_{Li^+}} \nabla \mu_{Li}$$

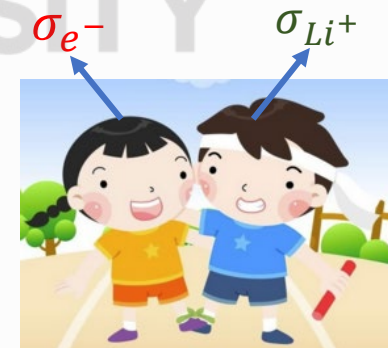
Compare:  $J_i = -\frac{\sigma_i}{z_i^2 F^2} \nabla \tilde{\mu}_i$

We have reached a simple yet somewhat expected result:

$$" \sigma_{Li} " = \frac{\sigma_{e^-} \sigma_{Li^+}}{\sigma_{e^-} + \sigma_{Li^+}} = \frac{1}{1/\sigma_{e^-} + 1/\sigma_{Li^+}}$$

Chemical diffusivity is limited by the species that move **more slowly**

If  $\sigma_{e^-} \gg \sigma_{Li^+}$ , then  $" \sigma_{Li} " \approx \sigma_{Li^+}$

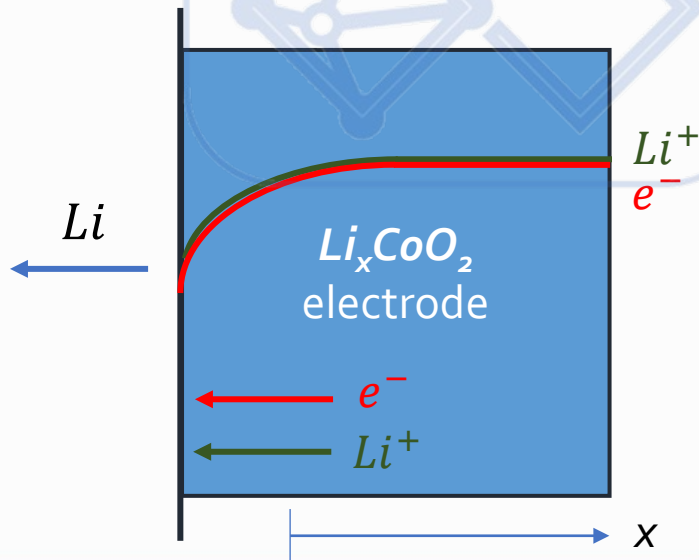


# How to solve for chemical diffusivity?

## Fick's first law

$$J_{diff, Li} = -D_{Li} \nabla c_{Li}$$

How to express  $D_{Li}$  as a function of  $D_{Li^+}$  and  $D_{e^-}$ ?



$$J_{Li} = -\frac{1}{F^2} \frac{\sigma_{e^-} \sigma_{Li^+}}{\sigma_{e^-} + \sigma_{Li^+}} (\nabla \tilde{\mu}_{e^-} + \nabla \tilde{\mu}_{Li^+})$$

$$\nabla c_{e^-} = \nabla c_{Li^+} = \nabla c_{Li}$$

$$= -\frac{RT}{F^2} \frac{\sigma_{e^-} \sigma_{Li^+}}{\sigma_{e^-} + \sigma_{Li^+}} \left( \frac{1}{c_{e^-}} + \frac{1}{c_{Li^+}} \right) \nabla c_{Li} \quad (\text{Dilute limit})$$

$D_{Li}^\delta$   $\delta$  means it describes the change of **non-stoichiometry**

$$D_{Li}^\delta = \frac{RT}{F^2} \frac{\sigma_{e^-} \sigma_{Li^+}}{\sigma_{e^-} + \sigma_{Li^+}} \underbrace{\left( \frac{1}{c_{e^-}} + \frac{1}{c_{Li^+}} \right)}_{\frac{1}{R^\delta}} \quad \text{So-called "chemical diffusivity"}$$

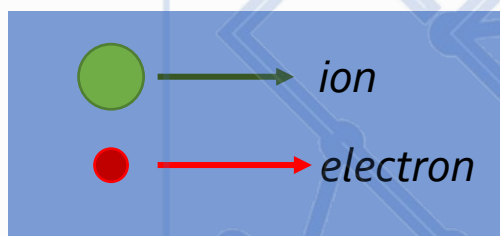
"Chemical Resistance" "Chemical Capacitance"

$$\text{Relaxation time } \tau^\delta = R^\delta C^\delta \propto \frac{L^2}{D_{Li}^\delta}$$

For  $D^\delta = 10^{-10} \text{ cm}^2/\text{s}$

$L$	$\tau$
10 mm	300 years
10 $\mu\text{m}$	2 hours
10 nm	0.01 s

Mixed ionic & electronic conductor (MIEC)

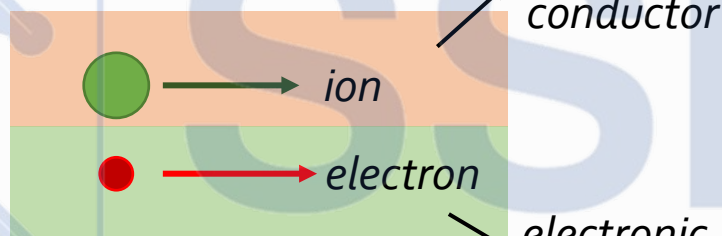


Chemical diffusion

$$\frac{1}{R\delta} = \frac{\sigma_{eon}\sigma_{ion}}{\sigma_{eon} + \sigma_{ion}}$$

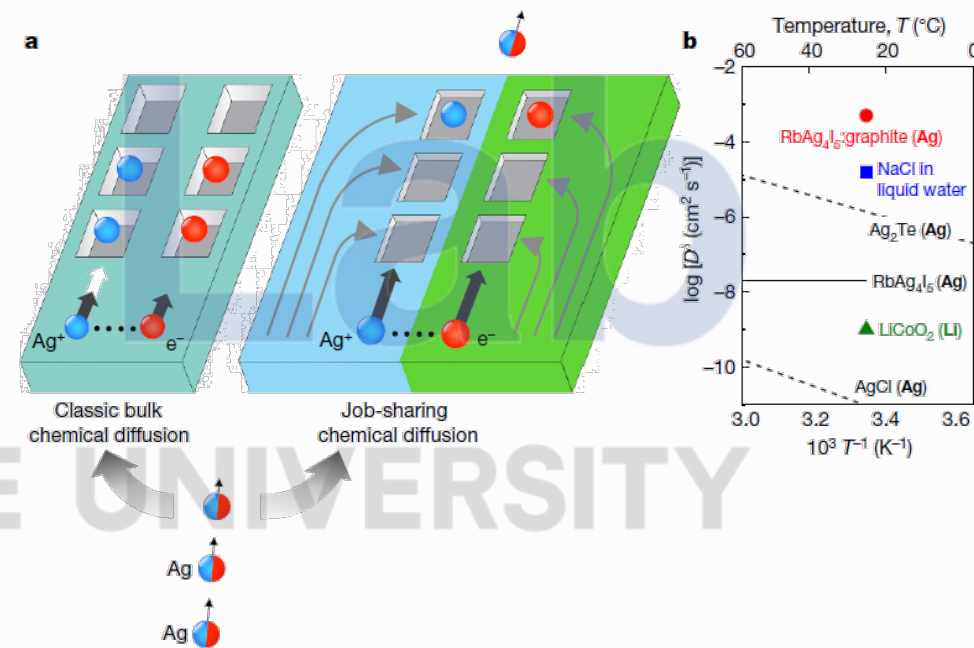
$$D^{\delta} \propto \frac{1}{R\delta}$$

"Job-sharing" conductors (?)



$$\frac{1}{R\delta} = ???$$

$$D^{\delta'} \gg D^{\delta} ???$$



Chia-Chin Chen, Lijun Fu & Joachim Maier, *Nature* (2016)

## Type of diffusivities:

- What are the different types of diffusivities?
- What physical mechanism and concept does each diffusivity describe?

## Chemical diffusivity:

- What physical process does the chemical diffusion describe?
- What are the key factors that govern the chemical diffusivity?

**Goal of this lecture:** you should be able to answer the questions above now (hopefully) : )

# End of Lecture 5

## Solid State Ionics Fall 2022

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